

B.Sc. III, PAPER-5Langmuir adsorption isotherm equation -

Freundlich adsorption isotherm is valid only on certain range of pressure only. To solve this difficulty Langmuir gave an adsorption isotherm which is called Langmuir adsorption isotherm. Following are main assumption for Langmuir adsorption isotherm.

- (a) The adsorbed layer is unimolecular and not multilayer. This occurs at low pressure or at moderately high temperature.
- (b) The adsorption is taking place on the fixed site of the surface and there is no any vander waal forces between adsorbate molecules to form multilayer. On site adsorbs only one ~~one~~ molecule when whole surface is covered by adsorbate molecule, a saturation state is established and then there is no further adsorption.
- (c) The adsorption is dynamic in nature i.e. condensation process and evaporation of adsorbate molecule occurs ~~and~~ simultaneously and at equilibrium.

$$\text{Rate of condensation} = \text{Rate of evaporation}$$

- (e) Gas molecule behaves ideally.
 (f) Surface of solid is uniform energetically.

Derivation of Langmuir adsorption isotherm:

Let

θ = the fraction of the surface of adsorbent covered by adsorbate at a time t .

$\therefore 1 - \theta$ = will be fraction of ~~are~~ bare and available for adsorption.

P = Pressure of gas.

Then according to Langmuir theory of adsorption.

Rate of condensation $\propto (1 - \theta)P$

or Rate of condensation = $K_1(1 - \theta)P$ — (i)

Here K_1 = Proportionality constant

and Rate of evaporation $\propto \theta$

= $K_2\theta$ — (ii)

K_2 = proportionality constant

At equilibrium.

Rate of condensation

= Rate of evaporation

From eqn (i) and (ii)

$$\Rightarrow K_1(1 - \theta)P = K_2\theta \text{ — (iii)}$$

$$\text{or } k_1 P - k_1 \theta P = k_2 \theta$$

$$\text{or } k_1 P = \theta (k_2 + k_1 P)$$

$$\text{or } \theta = \frac{k_1 P}{k_2 + k_1 P}$$

$$\text{or } \theta = \frac{\frac{k_1}{k_2} P}{1 + \frac{k_1}{k_2} P} = \frac{bP}{1 + bP} \quad \text{(iv)}$$

$$\text{Where } b = \frac{k_1}{k_2}$$

If x = amount of adsorbate and m = amount of adsorbent - then considering unimolecular lay adsorption, the gas adsorbed per unit area or per gram of adsorbent will be proportional to surface area covered at any time.

$$\frac{x}{m} \propto \theta$$

$$\text{or } \frac{x}{m} = k_3 \theta \quad \text{(v)}$$

k_3 - proportionality constant

Putting value of θ from eqⁿ (iv) in eqⁿ (v)

$$\frac{x}{m} = k_3 \cdot \frac{bP}{1 + bP}$$

$$\text{or } \frac{x}{m} = \frac{k_3 b P}{1 + b P} = \frac{a P}{1 + b P} \quad \text{(vi)}$$

Where $a = k_3 b$.

Equation (vi) is known as Langmuir adsorption isotherm.

~~The reciprocal of eqn (vi) is~~

eq (vi) is divided by p , then

$$\frac{x/m}{p} = \frac{a}{1+bp}$$

reciprocal of this equation

$$\frac{p}{x/m} = \frac{1+bp}{a}$$

$$\text{or } \frac{p}{x/m} = \frac{1}{a} + \frac{b}{a}p$$

Plotting Here, a, b are constant, hence

Plotting graph of $p/x/m$ versus p will be a straight line, the value of slope will be equal to b/a and intercept at y axis will give value of $\frac{1}{a}$